

Approximation Algorithms

FIND-VERTEX-COVER: given undirected G , output smallest vertex cover
a 2-approximation algorithm

APPROX-FIND-VERTEX-COVER(G)

INVARIANT: a) $|C| \leq 2|A|$

b) edges in A have

Basis: a) $|C| \leq 2|A|$ b)

Maintenance: a)

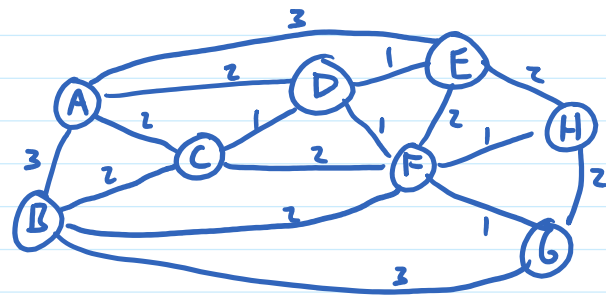
b)

Termination:

Approximate TSP

FIND-TSP- Δ : Given weighted undirected G that satisfies triangle inequality, find lowest weight tour.

APPROX-FIND-TSP- Δ



General TSP is not 2-approximable

HC(G)

1) Build complete G' with same vertices as G

$$\text{Set } w(u,v) = \begin{cases} 1 & \text{if } (u,v) \text{ in } G \\ 2 & \text{otherwise} \end{cases}$$

2)

3)

if G has HC then G' has tour of cost

if G has no HC then optimal tour in G' has cost

Randomized Algorithms

\rightarrow distinct
SELECT(S, k)

Let $X =$ total number of steps

$X_i =$ total number of steps in phase i

$X =$

$E[X] =$