YALE UNIVERSITY DEPARTMENT OF COMPUTER SCIENCE

CPSC 367: Cryptography and Computer Security

Professor M. J. Fischer

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Homework Assignment 4

Due: Tuesday, February 12, 2019

The goal of this assignment is to test your understanding of the concepts of block cipher, information leakage, and perfect security.

Twister

Twister is a block cipher on 3-letter blocks. It uses both substitution and transposition. The message space \mathcal{M} and ciphertext space \mathcal{C} are triples of letters, encoded by numbers in the range [0..25] as with the Caesar cipher. The key space $\mathcal{K} = \{0, \ldots, 77\}$. Note that $|\mathcal{K}| = 78 = 26 \times 3$.

Twister encryption is the composition of two ciphers E_k^1 and E_k^2 , so $E_k = E_k^2 \circ E_k^1$. The first cipher,

$$E_k^1(m_1, m_2, m_3) = ((m_1 + k) \mod 26, (m_2 + k) \mod 26, (m_3 + k) \mod 26),$$

is the shift substitution used by the Caesar cipher, applied separately to each letter of the message block (m_1, m_2, m_3) . The second cipher,

$$E_k^2(m_1, m_2, m_3) = (m_1', m_2', m_3'),$$

is a transposition cipher, where the letter in position j is moved to position $t_k(j)$, where $t_k(j) = ((j+k-1) \mod 3) + 1$. Thus, $m'_{t_k(j)} = m_j$,

Questions:

- 1. How does one decrypt Twister?
- 2. Is Twister information-theoretically secure? Why or why not?
- 3. How much does increasing the key space to $\{0, \ldots, 155\}$ increase the difficulty of breaking Twister?
- 4. What is the effect on security of increasing the key space to $\{0, \ldots, 78\}$?

Please answer questions 3 and 4 with respect to both information leakage and to the difficulty of carrying out a brute-force attack. As usual, we assume keys are chosen uniformly at random from the key space.