

Lecture Notes 1

1 Course Overview

This course is about cryptography and its application to computer and network security. A better term might be *information security*, which includes all forms of information protection, whether the information resides in a computer, on the network, or on a storage device such as a hard disk, DVD, or even paper. Security is a huge field and includes important non-technical topics such as incentive, opportunity, deterrence, threat, trust, anonymity, and coercion, all of which play together into the overall security picture. Our focus is on a particular set of useful tools—cryptographic primitives—that that can be used to enhance information security. Nevertheless, we need some awareness of general security issues in order to understand the environment in which cryptographic tools are used and to motivate the properties that we desire of these tools.

2 Information Security

The classical information security problem is how to send secret messages over an insecure channel. But information security is much broader than this. It is also about preventing hackers from breaking into a computer, preventing denial of service attacks against web servers, preventing unauthorized modification of databases, preventing illegal copying of data, preventing fraud in e-commerce applications, and so forth.

Security generally seems to mean preventing bad things from happening. However, it is not always so easy to decide exactly what are the bad things that one is trying to prevent. Without knowing exactly *what* is to be prevented, one can never know how *effective* a security system is at preventing them. This leads to the analysis of *attack scenarios*—the things an adversary might attempt that we'd like to protect against. Of course, one also wants to allow those activities to proceed normally that are not proscribed by the security policy.

2.1 A security example from real life

A familiar example of a security problem is that of keeping intruders out of my house.

What do I want to keep out? Specifying exactly what is to be kept out and what allowed is already not such an easy problem. At first sight, I might say that I don't want anybody entering whom I have not specifically authorized. But even this can be a bit problematical.

1. Do I also want to prevent chimpanzees from entering?
2. Do I want to prevent mice from entering?
3. Do I want to prevent the twin brother of my friend Alex from entering (who looks so much like Alex that even I can't always tell them apart)?

While these questions may sound silly, they have serious analogs in information security. To (1), you'd likely say, "Of course, I don't want to let chimpanzees in the house either, but I don't consider them a threat because there are no chimpanzees in my neighborhood." Yet the world of information security is replete with examples of security holes that are of no consequence until someone develops an exploit, at which time they suddenly become serious problems. To (2), you might say, "No, I don't want mice in, either", but at the same time you'd realize that the means of preventing mice from entering are quite different from those of protecting against human intruders, and conflating the two problems will only make finding workable solutions that much harder. To (3), you're forced to think about the meaning of identity. What is it about Alex that makes me want to let him in but not his twin brother? What hope do I have of solving this problem if I can't distinguish between the two? In fact, the simple solution of giving Alex a key to the house works in practice, as long as I know that it is Alex getting the key and not his brother. Distinguishing among individuals becomes a serious problem on the internet, and schemes purporting to identify individuals generally identify instead possession of secret information (a cryptographic key) or a particular object (such as a smart card) instead, with the assumption that this is sufficient to identify the individual. It isn't always so in the real world, for secrets can be stolen and smart cards forged. The rapid growth of identity theft today is evidence of this fact. (See <http://www.consumer.gov/idtheft/> for further information on this topic.)

What are some possible means to keep out intruders, and how effective are they? We now look at some of the means that might be used to keep intruders out and discuss their effectiveness.

1. Post a "no trespassing – do not enter" sign.
2. Lock the front door.
3. Install a burglar alarm.
4. Buy a gun.
5. Call the police.
6. Sue the intruder.
7. Conceal the entrance.

Think carefully about each of these means and ask yourself under what conditions it might be effective, and what else must be in place for it to work. For example, suing the intruder presupposes that he can be identified, that you have evidence that he entered illegally, and that society has an effective judicial system. Buying a gun will only deter breakins if it is known that you are likely to possess a gun. Locking the front door has little effect unless the back door and windows are also locked.

2.2 Cryptography and security

Cryptography is to information security as locks are to personal security.

- Both are clever mechanisms that can be analyzed in isolation.
- Both can be effective when used in suitable contexts.
- Both comprise only a small part of the security picture.

2.3 Information security in the real world

Here are just some of the many goals of information security.

- Protection against data damage.
- Protection against theft of intellectual property.
- Protection against surveillance.
- Protection against unauthorized actions.
- Protection of constitutional privacy rights.
- Protection of freedom of information.

How is security achieved in the real world?

- **Prevention:** Physical barriers, locks, encryption, firewalls, etc.
- **Detection:** Audits, checks and balances.
- **Legal means:** Laws, sanctions.
- **Concealment:** Camouflage, steganography.

Absolute security in the real world is infeasible. The goal is risk management. The same is true with information security. Security mechanisms have a cost. One needs to weight their cost against the benefits.

3 Organization

The course will be roughly organized around *cryptographic primitives*, objects having properties that make them useful in solving certain security problems. For each such primitive, one can ask:

What can be done with it? This leads to a study of cryptographic algorithms and protocols.

What are its properties? This leads to modeling and analysis, which very quickly requires complexity theory, probability theory, and statistics.

How is it built? This requires a fair amount of mathematics, particularly number theory and algebra. Don't worry if you haven't studied these topics before. We will cover what is need for the methods discussed in this course.

How is it implemented? Implementing cryptographic primitives requires a lot of attention to detail, especially to make sure that the programs don't accidentally leak secret information. This course will involve some implementation.

4 Computer Science, Mathematics and Cryptography

Cryptography cuts across subareas of both computer science and mathematics. On the computer science side, cryptographic algorithms and protocols not only carry out sophisticated distributed computations, but they must be implemented in a way so as to not inadvertently leak sensitive information. It doesn't matter how mathematically strong the mathematical primitive is if a sloppy implementation allows an adversary to discover the key. There will be some implementation problems to give you a flavor of what it is like to program cryptographic algorithms.

Mathematics enters the field at several levels. Many cryptographic primitives are based on number theoretic problems such as factoring and discrete log and on algebraic properties of structures such as elliptic curves. Understanding and modeling security uses probability theory and coding theory on the one hand, and complexity theory on the other. We will explore these topics in enough depth to give you some understanding into how various cryptographic primitives work and why they are believed to be secure.

5 Example primitive: Symmetric cryptography

A *symmetric cryptosystem* (sometimes called a *private-key* or *one-key* system) is a pair of efficiently-computable functions E and D such that $D(k, E(k, m)) = m$ for all keys k and all messages m . Moreover, given $c = E(k, m)$, it is hard to find m without knowing the key k .

5.1 What can be done with a symmetric cryptosystem?

This is the classical tool for solving the *secret message transmission problem*:

1. Alice wants to send Bob a private message m over the internet.
2. Alice and Bob both have a secret key k .
3. Alice computes $c = E(k, m)$ and sends c to Bob.
4. Bob receives c' , computes $m' = D(k, c')$, and assumes m' to be Alice's message. [What happens if $c' \neq c$?]

We assume that the network is insecure and that an eavesdropper, Eve, can listen in and learn c . We desire nonetheless that m remain private and unknown to Eve.

5.2 What do we require of E , D , and the computing environment in order for this protocol to accomplish Alice and Bob's goals?

- Given c , it is hard to find m without also knowing k .
- k is not initially known to Eve.
- Eve can guess k with at most an extremely tiny probability of success. This means k must be chosen randomly from a large key space.
- Alice and Bob protect k from being released. Their computers have not been compromised. Eve is not able to obtain k by looking on Alice's or Bob's hard disk, swap file, or free memory pages, even if she is a legitimate user of that computer or the services it provides.

- There are no unanticipated ways by which Eve succeeds in obtaining k , e.g., social engineering, using binoculars to watch Alice or Bob's keyboard, etc. etc.