CPSC 467: Cryptography and Computer Security

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Outline

Advanced Encryption Standard (cont.)

AES Alternatives

Chaining Modes
Block chaining modes
Extending chaining modes to bytes

Public-key Cryptography

RSA

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Advanced Encryption Standard (cont.)

Outline

Public-key

Hardware Support for AES

Both Intel and AMD provide a set of instructions for AES promising 3x to 10x acceleration versus pure software implementation.

- AESENC/AESDEC one round of encryption / decryption
- AESENCLAST/AESDECLAST last round of encryption / decryption
- AESKEYGENASSIST key expansion

Breaking AES

Outline

The ability to recover a key from known or chosen ciphertext(s) with a reasonable time and memory requirements.

Frequently, reported attacks are attacks on the implementation, not the actual cipher:

- ▶ Buggy implementation of the cipher (e.g., memory leakage)
- ► Side channel attacks (e.g., time and power consumption analysis, electromagnetic leaks)
- Weak key generation (e.g., bad PRBGs, attacks on master passwords)
- Key leakage (e.g., a key saved to a hard drive)

Public-key

Appendix

AES Security: Keys

Certain ciphers (e.g., DES, IDEA, Blowfish) suffer from weak keys.

A weak key¹ is a key that makes a cipher behave in some undesirable way. A cipher with no weak keys is said to have a *flat*, or *linear*, key space.

DES, unlike AES, suffers from weak keys (alternating 0's and 1's, F's and E's, E's and 0's, 1's and F's).

DES weak keys produce 16 identical subkeys.

Q: Why are DES weak keys a problem?

Wikipedia: Weak Keys

AES Security

Outline

Attacks have been published that are computationally faster than a full brute force attack

Q: What is the complexity of a brute force attack on AES-128?

AES Security

Outline

All known attacks are computationally infeasible.

Interesting results:

▶ Best key recovery attack: AES-128 with computational complexity 2^{126.1}; AES-192, 2^{189.7}; and AES-256, 2^{254.4}.

A. Bogdanov, D. Khovratovich and C. Rechberger, Biclique Cryptanalysis of the Full AES, ASIACRYPT 2011

▶ Related-key attack on AES-256 with complexity 2⁹⁹ given 2⁹⁹ plaintext/ciphertext pairs encrypted with four related keys.

A. Biryuko and D. Khovratovich, Related-key Cryptanalysis of the Full AES-192 and AES-256, ASIACRYPT 2009

AES Security

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Allegedly, NSA is actively looking for ways to break AES.

"Prying Eyes: Inside the NSA's War on Internet Security", Spiegiel, 12/2014

(TS//SI//REL) TUNDRA -- Electronic codebooks, such as the Advanced Encryption Standard, are both widely used and difficult to attack cryptanalytically. NSA has only a handful of in-house techniques. The TUNDRA project investigated a potentially new technique -- the Tau statistic -- to determine its usefulness in codebook analysis. This project was supported by

Bruce Schneier on AES security²

"I don't think there's any danger of a **practical** attack against AES for a long time now. Which is why the community should start thinking about migrating now" (2011)

"Cryptography is all about **safety margins**. If you can break n round of a cipher, you design it with 2n or 3n rounds. At this point, I suggest AES-128 at 16 rounds, AES-192 at 20 rounds, and AES-256 at 28 rounds. Or maybe even more; we don't want to be revising the standard again and again" (2009)

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²Bruce Schneier's Blog http://www.schneier.com/blog/archives/2011/08/new_attack_on_a_1.html

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Other ciphers

There are many good block ciphers to choose from:

 Blowfish, Serpent, Twofish, Camellia, CAST-128, IDEA, RC2/RC5/RC6, SEED, Skipjack, TEA, XTEA

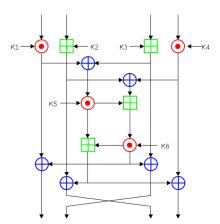
We will have a brief look at

- ► IDEA
- Blowfish
- RC6
- ► TFA

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- Invented by James Massey
- Supports 64-bit data block and 128-bit key
- ▶ 8 rounds
- ▶ Novelty: Uses mixed-mode arithmetic to produce non-linearity
 - Addition mod 2 combined with addition mod 2¹⁶
 - ► Lai-Massey multiplication ~multiplication mod 2¹⁶
- No explicit S-boxes required



multiplication modulo $2^{16} + 1$ bitwise XOR addition modulo 2^{16}

 $Image\ retrieved\ from\ http://en.wikipedia.org/wiki/International_Data_Encryption_Algorithm$

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Blowfish

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- Invented by Bruce Schneier
- Supports 64-bit data block and a variable key length up to 448 bits
- ▶ 16 rounds
- ▶ Round function uses 4 S-boxes which map 8 bits to 32 bits
- ▶ Novelty: the S-boxes are key-dependent (determined each time by the key)

RC₆

Outline

- Invented by Ron Rivest
- ▶ Variable block size, key length, and number of rounds
- Compliant with the AES competition requirements (AES finalist)
- Novelty: data dependent rotations
 - Very unusual to rely on data

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TEA (Tiny Encryption Algorithm)

- Invented by David Wheeler and Roger Needham
- Supports 64-bit data block and 128-bit key
- Variable number of rounds (64 rounds suggested)
 - "Weak" round function, hence large number of rounds
- ▶ Novelty: extremely simple, efficient and easy to implement

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TEA Encryption(32 rounds)

```
(K[0], K[1], K[2], K[3]) = 128 bit key
(L, R) = plaintext (64-bit block)
delta = 0x9e3779b9
s_{11m} = 0
for i = 1 to 32
    sum = sum + delta
    L = L + (((R \ll 4) + K[0]) \oplus (R + \text{sum}) \oplus ((R \gg 5) + K[1]))
    R = R + (((L \ll 4) + K[2]) \oplus (L + sum) \oplus ((L \gg 5) + K[3]))
next i
ciphertext = (L, R)
```

Tea Decryption

```
(K[0], K[1], K[2], K[3]) = 128 bit key
(L,R) = ciphertext (64-bit block)
delta = 0x9e3779b9
sum = delta << 5
for i = 1 to 32
    R = R - (((L \ll 4) + K[2]) \oplus (L + sum) \oplus ((L \gg 5) + K[3]))
    L = L - (((R \ll 4) + K[0]) \oplus (R + sum) \oplus ((R \gg 5) + K[1]))
    sum = sum - delta
next i
plaintext = (L, R)
```

Figures retrieved from Information Security Principles and Practice, Mark Stamp, Wiley, 2006

Chaining Modes

Encrypting sequences of blocks in ECB mode

Recall from <u>lecture 6</u>: A *chaining mode* tells how to encrypt a sequence of plaintext blocks m_1, m_2, \ldots, m_t to produce a corresponding sequence of ciphertext blocks c_1, c_2, \ldots, c_t , and conversely, how to recover the m_i 's given the c_i 's.

Electronic Code Book (ECB) mode encrypts/decrypts each block separately.

$$c_i = E_k(m_i), 1 \leq i \leq t.$$

Block chaining modes

Outline

Encrypting sequences of blocks in OFB mode

Output Feedback (OFB) mode repeatedly applies the block cipher to a fixed initialization vector (IV) to produce a sequence of subkeys. Each block is encrypted/decrypted by XORing with the corresponding subkey.

$$k_0 = E_k(IV)$$

 $k_i = E_k(k_{i-1}), c_i = m_i \oplus k_i, 1 \le i \le t.$

Block chaining modes

Outline

Removing cipher block dependence from ECB

ECB has the undesirable property that identical plaintext blocks yield identical ciphertext blocks.

Cipher Block Chaining Mode (CBC) breaks this relationship by mixing in the previous ciphtertext block when encrypting the current block.

- \triangleright To encrypt, Alice applies E_k to the XOR of the current plaintext block with the previous ciphertext block. That is, $c_i = E_k(m_i \oplus c_{i-1})$.
- ▶ To decrypt, Bob computes $m_i = D_k(c_i) \oplus c_{i-1}$.

To get started, we take $c_0 = IV$, where IV is a fixed *initialization vector* which we assume is publicly known.

Outline

Removing cipher block dependence from OFB

OFB has the undesirable property that two messages with identical plaintext blocks in corresponding block positions will yield identical ciphertext blocks in those same positions.

Cipher Feedback (CFB) mode breaks this relationship by choosing the current subkey k_i to be the encryption of the previous ciphertext block c_{i-1} rather than as the encryption of the previous subkey as is done with OFB.

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Cipher Feedback (CFB)

- ▶ To encrypt, Alice computes $k_i = E_k(c_{i-1})$ and $c_i = m_i \oplus k_i$. c_0 is a fixed initialization vector.
- ▶ To decrypt, Bob computes $k_i = E_k(c_{i-1})$ and $m_i = c_i \oplus k_i$.

Note that Bob is able to decrypt without using the block decryption function D_k . In fact, it is not even necessary for E_k to be a one-to-one function (but using a non one-to-one function might weaken security).

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OFB, CFB, and stream ciphers

Both OFB and CFB are closely related to stream ciphers. In both cases, $c_i = m_i \oplus k_i$, where subkey k_i is computed from the master key and the data that came before stage i.

Like a one-time pad, OFB is insecure if the same key is ever reused, for the sequence of k_i 's generated will be the same. If m and m' are encrypted using the same key k, then $m \oplus m' = c \oplus c'$.

CFB partially avoids this problem, for even if the same key k is used for two different message sequences m_i and m_i' , it is only true that $m_i \oplus m_i' = c_i \oplus c_i' \oplus E_k(c_{i-1}) \oplus E_k(c_{i-1}')$, and the dependency on k does not drop out. However, the problem still exists when m and m' share a prefix.

Propagating Cipher-Block Chaining Mode (PCBC)

Here is a more complicated chaining rule that nonetheless can be deciphered.

- To encrypt, Alice XORs the current plaintext block, previous plaintext block, and previous ciphertext block. That is, $c_i = E_k(m_i \oplus m_{i-1} \oplus c_{i-1})$. Here, both m_0 and c_0 are fixed initialization vectors.
- ▶ To decrypt, Bob computes $m_i = D_k(c_i) \oplus m_{i-1} \oplus c_{i-1}$.

Outline

Recovery from data corruption

In real applications, a ciphertext block might be damaged or lost. An interesting property is how much plaintext is lost as a result.

- ▶ With ECB and OFB, if Bob receives a bad block c_i, then he cannot recover the corresponding m_i , but all good ciphertext blocks can be decrypted.
- ▶ With CBC and CFB, Bob needs good c_i and c_{i-1} blocks in order to decrypt m_i . Therefore, a bad block c_i renders both m_i and m_{i+1} unreadable.
- ▶ With PCBC, bad block c_i renders m_i unreadable for all $i \geq i$.

Error-correcting codes applied to the ciphertext are often used in practice since they minimize lost data and give better indications of when irrecoverable data loss has occurred.

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Other modes

Other modes can easily be invented.

In all cases, c_i is computed by some expression (which may depend on i) built from $E_k()$ and \oplus applied to available information:

- ciphertext blocks c_1, \ldots, c_{i-1} ,
- ▶ message blocks m_1, \ldots, m_i ,
- any initialization vectors.

Any such equation that can be "solved" for m_i (by possibly using $D_k()$ to invert $E_k()$) is a suitable chaining mode in the sense that Alice can produce the ciphertext and Bob can decrypt it.

Of course, the resulting security properties depend heavily on the particular expression chosen.

Byte chaining modes

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Stream ciphers from OFB and CFB block ciphers

OFB and CFB block modes can be turned into stream ciphers.

Both compute $c_i = m_i \oplus k_i$, where

- \triangleright $k_i = E_k(k_{i-1})$ (for OFB);
- $\qquad \qquad k_i = E_k(c_{i-1}) \text{ (for CFB)}.$

Assume a block size of b bytes. Number the bytes in block m_i as $m_{i,0}, \ldots, m_{i,b-1}$ and similarly for c_i and k_i .

Then $c_{i,j} = m_{i,j} \oplus k_{i,j}$, so each output byte $c_{i,j}$ can be computed before knowing $m_{i,j'}$ for j' > j; no need to wait for all of m_i .

One must keep track of j. When j = b, the current block is finished, i must be incremented, j must be reset to 0, and k_{i+1} must be computed.

Byte chaining modes

Extended OFB and CFB modes

Simpler (for hardware implementation) and more uniform stream ciphers result by also computing k_i a byte at a time.

The idea: Use a shift register X to accumulate the feedback bits from previous stages of encryption so that the full-sized blocks needed by the block chaining method are available.

X is initialized to some public initialization vector.

Details are in the appendix.

Public-key Cryptography

Public-key

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Public-key cryptography

Classical cryptography uses a single key for both encryption and decryption. This is also called a *symmetric* or 1-key cryptography.

There is no logical reason why the encryption and decryption keys should be the same.

Allowing them to differ gives rise to asymmetric cryptography, also known as *public-key* or *2-key* cryptography.

Asymmetric cryptosystems

An asymmetric cryptosystem has a pair $k = (k_e, k_d)$ of related keys, the encryption key k_e and the decryption key k_d .

Alice encrypts a message m by computing $c = E_{k_a}(m)$. Bob decrypts c by computing $m = D_{k_d}(c)$.

We sometimes write e and d as shorthand for k_e and k_d , respectively.

As always, the decryption function inverts the encryption function, so $m = D_d(E_e(m))$.

Security requirement

Should be hard for Eve to find m given $c = E_e(m)$ and e.

- ► The system remains secure even if the encryption key *e* is made public!
- *e* is said to be the *public key* and *d* the *private key*.

Reason to make e public.

- Anybody can send an encrypted message to Bob. Sandra obtains Bob's public key e and sends $c = E_e(m)$ to Bob.
- ▶ Bob recovers m by computing $D_d(c)$, using his private key d.

This greatly simplifies key management. No longer need a secure channel between Alice and Bob for the initial key distribution (which I have carefully avoided talking about so far).

Public-key

An active adversary Mallory can carry out a nasty man-in-the-middle attack.

- Mallory sends his own encryption key to Sandra when she attempts to obtain Bob's key.
- ▶ Not knowing she has been duped, Sandra encrypts her private data using Mallory's public key, so Mallory can read it (but Bob cannot)!
- ► To keep from being discovered, Mallory intercepts each message from Sandra to Bob, decrypts using his own decryption key, re-encrypts using Bob's public encryption key, and sends it on to Bob. Bob, receiving a validly encrypted message, is none the wiser.

Public-key

Passive attacks against a 2-key cryptosystem

Making the encryption key public also helps a passive attacker.

- 1. Chosen-plaintext attacks are always available since Eve can generate as many plaintext-ciphertext pairs as she wishes using the public encryption function $E_e()$.
- 2. The public encryption function also gives Eve a foolproof way to check validity of a potential decryption. Namely, Eve can verify $D_d(c) = m_0$ for some candidate message m_0 by checking that $c = E_e(m_0)$.

Redundancy in the set of meaningful messages is no longer necessary for brute force attacks.

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Facts about asymmetric cryptosystems

Good asymmetric cryptosystems are much harder to design than good symmetric cryptosystems.

All known asymmetric systems are orders of magnitude slower than corresponding symmetric systems.

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Public-key

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Asymmetric and symmetric cryptosystems are often used together. Let (E^2, D^2) be a 2-key cryptosystem and (E^1, D^1) be a 1-key cryptosystem.

Here's how Alice sends a secret message m to Bob.

- ▶ Alice generates a random *session key k*.
- Alice computes $c_1 = E_k^1(m)$ and $c_2 = E_e^2(k)$, where e is Bob's public key, and sends (c_1, c_2) to Bob.
- ▶ Bob computes $k = D_d^2(c_2)$ using his private decryption key d and then computes $m = D_k^1(c_1)$.

This is much more efficient than simply sending $E_e^2(m)$ in the usual case that m is much longer than k.

Note that the 2-key system is used to encrypt random strings!

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Overview of RSA

Probably the most commonly used asymmetric cryptosystem today is RSA, named from the initials of its three inventors, Rivest, Shamir, and Adelman.

Unlike the symmetric systems we have been talking about so far, RSA is based not on substitution and transposition but on arithmetic involving very large integers—numbers that are hundreds or even thousands of bits long.

To understand why RSA works requires knowing a bit of number theory. However, the basic ideas can be presented guite simply, which I will do now.

Public-key

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RSA spaces

The message space, ciphertext space, and key space for RSA is the set of integers $\mathbf{Z}_n = \{0, \dots, n-1\}$ for some very large integer n.

For now, think of n as a number so large that its binary representation is 1024 bits long.

Such a number is unimaginably big. It is bigger than $2^{1023} \approx 10^{308}$.

For comparison, the number of atoms in the observable universe³ is estimated to be "only" 10^{80} .

³Wikipedia, https://en.wikipedia.org/wiki/Observable_universe

Public-key

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To use RSA as a block cipher on bit strings, Alice must convert each block to an integer $m \in \mathbf{Z}_n$, and Bob must convert m back to a block.

Many such encodings are possible, but perhaps the simplest is to prepend a "1" to the block x and regard the result as a binary integer *m*.

To decode m to a block, write out m in binary and then delete the initial "1" bit.

To ensure that m < n as required, we limit the length of our blocks to 1022 bits.

RSA

Here's how Bob generates an RSA key pair.

AES Alternatives

- Bob chooses two sufficiently large distinct prime numbers p and q and computes n = pq. For security, p and q should be about the same length (when written in binary).
- ▶ He computes two numbers e and d with a certain number-theoretic relationship.
- ▶ The public key is the pair $k_e = (e, n)$. The private key is the pair $k_d = (d, n)$. The primes p and q are no longer needed and should be discarded.

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RSA encryption and decryption

To encrypt, Alice computes $c = m^e \mod n$. ⁴

To decrypt, Bob computes $m = c^d \mod n$.

Here, $a \mod n$ denotes the remainder when a is divided by n.

This works because e and d are chosen so that, for all m,

$$m = (m^e \bmod n)^d \bmod n. \tag{1}$$

Public-key

That's all there is to it, once the keys have been found.

Most of the complexity in implementing RSA has to do with key generation, which fortunately is done only infrequently.

⁴For now, assume all messages and ciphertexts are integers in \mathbf{Z}_n .

RSA questions

You should already be asking yourself the following questions:

- ▶ How does one find *n*, *e*, *d* such that (1) is satisfied?
- Why is RSA believed to be secure?

AES Alternatives

- ▶ How can one implement RSA on a computer when most computers only support arithmetic on 32-bit or 64-bit integers, and how long does it take?
- \triangleright How can one possibly compute m^e mod n for 1024 bit numbers. m^e , before taking the remainder, has size roughly

$$\left(2^{1024}\right)^{2^{1024}} = 2^{1024 \times 2^{1024}} = 2^{2^{10} \times 2^{1024}} = 2^{2^{1034}}.$$

This is a number that is roughly 2^{1034} bits long! No computer has enough memory to store that number, and no computer is fast enough to compute it.

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Details for extended modes

Assume block size b = 16 bytes.

Define two operations: L and R on blocks:

- \blacktriangleright L(x) is the leftmost byte of x;
- ▶ R(x) is the rightmost b-1 bytes of x.

Public-key

The extended versions of OFB and CFB are very similar.

Both maintain a one-block shift register X.

The shift register value X_s at stage s depends only on c_1, \ldots, c_{s-1} (which are now single bytes) and the master key k.

At stage i, Alice

- computes X_s according to Extended OFB or Extended CFB rules;
- ▶ computes byte key $k_s = L(E_k(X_s))$;
- encrypts message byte m_s as $c_s = m_s \oplus k_s$.

Bob decrypts similarly.

Shift register rules

The two modes differ in how they update the shift register.

Extended OFB mode

$$X_s = R(X_{s-1}) \cdot k_{s-1}$$

Extended CFB mode

$$X_s = R(X_{s-1}) \cdot c_{s-1}$$

('⋅' denotes concatenation.)

Summary:

- ▶ Extended OFB keeps the most recent *b* key bytes in *X*.
- ▶ Extended CFB keeps the most recent *b* ciphertext bytes in *X*,

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Public-key

Comparison of extended OFB and CFB modes

The differences seem minor, but they have profound implications on the resulting cryptosystem.

- ▶ In eOFB mode, X_s depends only on s and the master key k(and the initialization vector IV), so loss of a ciphertext byte causes loss of only the corresponding plaintext byte.
- ▶ In eCFB mode, loss of ciphertext byte c_s causes m_s and all succeeding message bytes to become undecipherable until c_s is shifted off the end of X. Thus, b message bytes are lost.

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The downside of eOFB is that security is lost if the same master key is used twice for different messages. CFB does not suffer from this problem since different messages lead to different ciphertexts and hence different keystreams.

Nevertheless, eCFB has the undesirable property that the keystreams are the same up to and including the first byte in which the two message streams differ.

This enables Eve to determine the length of the common prefix of the two message streams and also to determine the XOR of the first bytes at which they differ.

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Possible solution

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Possible solution to both problems: Use a different initialization vector for each message. Prefix the ciphertext with the (unencrypted) IV so Bob can still decrypt.